

A.- Hallar las siguientes integrales inmediatas o integrales por cambio de variable:

$$1) \int \frac{2}{\sqrt{x}} \cdot dx = 2 \int x^{-1/2} \cdot dx = 2 \cdot \frac{x^{1/2}}{1/2} + C = 4 \cdot \sqrt{x} + C$$

$$2) \int \frac{(\ln x)^8}{x} \cdot dx = \int (\ln x)^8 \cdot \frac{1}{x} \cdot dx = \frac{(\ln x)^9}{9} + C$$

$$3) \int \frac{x^2 - x^3 \cdot \operatorname{sen} x}{x^3} \cdot dx = \int \frac{x^2}{x^3} \cdot dx - \int \frac{x^3 \cdot \operatorname{sen} x}{x^3} \cdot dx = \int \frac{1}{x} \cdot dx - \int \operatorname{sen} x \cdot dx = \operatorname{Ln}|x| + \operatorname{cos} x + C$$

$$4) \int \frac{\sqrt[3]{x} + \sqrt{x}}{\sqrt[4]{x}} \cdot dx = \int \frac{x^{1/3}}{x^{1/4}} \cdot dx + \int \frac{x^{1/2}}{x^{1/4}} \cdot dx = \int x^{1/3-1/4} \cdot dx + \int x^{1/2-1/4} \cdot dx = \int x^{1/12} \cdot dx + \int x^{1/4} \cdot dx = \\ = \frac{x^{13/12}}{13/12} + \frac{x^{5/4}}{5/4} + C = \frac{13 \cdot \sqrt[12]{x^{13}}}{12} + \frac{4 \cdot \sqrt[4]{x^5}}{5} + C$$

$$5) \int \frac{1+2x}{1+x^2} \cdot dx = \int \frac{1}{1+x^2} \cdot dx + \int \frac{2x}{1+x^2} \cdot dx = \operatorname{arctg} x + \operatorname{Ln}(1+x^2) + C$$

$$6) \int 5x \cdot \sqrt{x^2 - 3} \cdot dx = \frac{5}{2} \cdot \int 2x \cdot (x^2 - 3)^{1/2} \cdot dx = \frac{5}{2} \cdot \frac{(x^2 - 3)^{3/2}}{3/2} + C = \frac{5 \cdot \sqrt{(x^2 - 3)^3}}{3} + C$$

$$7) \int x \cdot (3x^2 + 5)^{24} \cdot dx = \frac{1}{6} \cdot \int 6x \cdot (3x^2 + 5)^{24} \cdot dx = \frac{1}{6} \cdot \frac{(3x^2 + 5)^{25}}{25} + C = \frac{(3x^2 + 5)^{25}}{150} + C$$

$$8) \int \frac{1}{(x-4)^5} \cdot dx = \int (x-4)^{-5} \cdot dx = \frac{(x-4)^{-4}}{-4} + C = -\frac{1}{4 \cdot (x-4)^4} + C$$

$$9) \int \frac{4x^2}{\sqrt{5-x^3}} \cdot dx = \frac{4}{-3} \cdot \int -3x^2 \cdot (5-x^3)^{-1/2} \cdot dx = -\frac{4}{3} \cdot \frac{(5-x^3)^{1/2}}{1/2} + C = -\frac{8 \cdot \sqrt{5-x^3}}{3} + C$$

$$10) \int \frac{\cot gx}{\operatorname{sen}^2 x} \cdot dx = \int \cot gx \cdot \frac{1}{\operatorname{sen}^2 x} \cdot dx = - \int \cot gx \cdot \frac{-1}{\operatorname{sen}^2 x} \cdot dx = - \int t \cdot dt = -\frac{t^2}{2} + C = -\frac{\cot^2 gx}{2} + C \\ t = \cot gx \rightarrow dt = -\frac{1}{\operatorname{sen}^2 x} \cdot dx$$

$$11) \int \frac{3x}{x^2+5} \cdot dx = \frac{3}{2} \cdot \int \frac{2x}{x^2+5} \cdot dx = \frac{3}{2} \cdot \operatorname{Ln}(x^2+5) + C$$

$$12) \int \frac{x+1}{x^2+2x+5} \cdot dx = \frac{1}{2} \cdot \int \frac{2x+2}{x^2+2x+5} \cdot dx = \frac{1}{2} \cdot \operatorname{Ln}|x^2+2x+5| + C$$

$$13) \int \frac{5x^2}{\operatorname{sen}^2(x^3+5)} \cdot dx = \frac{5}{3} \int \frac{3x^2}{\operatorname{sen}^2(x^3+5)} \cdot dx = \frac{5}{3} \cdot (-\cot g(x^3+5)) + C = -\frac{5}{3} \cdot \cot g(x^3+5) + C$$

$$14) \int 3^{-3x+5} \cdot dx = \frac{1}{-3} \cdot \int 3^{-3x+5} \cdot (-3) \cdot dx = -\frac{1}{3} \cdot \frac{3^{-3x+5}}{\operatorname{Ln} 3} + C = -\frac{3^{-3x+5}}{3 \cdot \operatorname{Ln} 3} + C$$

$$15) \int 4x^2 \cdot e^{5x^3-3} \cdot dx = \frac{4}{15} \int 15x^2 \cdot e^{5x^3-3} \cdot dx = \frac{4}{15} \cdot e^{5x^3-3} + C = \frac{4e^{5x^3-3}}{15} + C$$

$$16) \int \cos(2x^3-5) \cdot 3x^2 \cdot dx = \frac{3}{6} \int \cos(2x^3-5) \cdot 6x^2 \cdot dx = \frac{1}{2} \cdot \operatorname{sen}(2x^3-5) + C = \frac{\operatorname{sen}(2x^3-5)}{2} + C$$

$$17) \int (1 + \operatorname{tg}^2(2x)) \cdot dx = \frac{1}{2} \cdot \int (1 + \operatorname{tg}^2(2x)) \cdot 2 \cdot dx = \frac{1}{2} \cdot \operatorname{tg}(2x) + C = \frac{\operatorname{tg}(2x)}{2} + C$$

$$18) \int \operatorname{tg}^2 x \cdot dx = \int (\operatorname{tg}^2 x + 1 - 1) \cdot dx = \int (\operatorname{tg}^2 x + 1) \cdot dx - \int 1 \cdot dx = \operatorname{tg} x - x + C$$

$$19) \int \frac{1}{1+9x^2} \cdot dx = \int \frac{1}{1+(3x)^2} \cdot dx = \frac{1}{3} \cdot \int \frac{3}{1+(3x)^2} \cdot dx = \frac{1}{3} \cdot \operatorname{arctg}(3x) + C$$

$$20) \int \frac{4}{49+x^2} \cdot dx = \int \frac{4/49}{1+x^2/49} \cdot dx = \frac{4}{49} \cdot 7 \cdot \int \frac{1/7}{1+(x/7)^2} \cdot dx = \frac{4}{7} \cdot \operatorname{arctg}\left(\frac{x}{7}\right) + C$$

$$21) \int \frac{1}{\sqrt{9-64x^2}} \cdot dx = \int \frac{1/\sqrt{9}}{\sqrt{1-64x^2/9}} \cdot dx = \frac{1}{8} \int \frac{8/3}{\sqrt{1-(8x/3)^2}} \cdot dx = \frac{1}{8} \cdot \operatorname{arcsen}\left(\frac{8x}{3}\right) + C$$

$$22) \int \frac{\operatorname{sen}\left(\frac{1}{x}\right)}{x^2} \cdot dx = \int \operatorname{sen}\left(\frac{1}{x}\right) \cdot \frac{1}{x^2} \cdot dx = - \int \operatorname{sen}\left(\frac{1}{x}\right) \cdot \frac{-1}{x^2} \cdot dx = - \left(-\cos\left(\frac{1}{x}\right) \right) + C = \cos\left(\frac{1}{x}\right) + C$$

$$23) \int \frac{\cos(\sqrt{x})}{3 \cdot \sqrt{x}} \cdot dx = \int \cos(\sqrt{x}) \cdot \frac{1}{3 \cdot \sqrt{x}} \cdot dx = \frac{2}{3} \cdot \int \cos(\sqrt{x}) \cdot \frac{1}{2 \cdot \sqrt{x}} \cdot dx = \frac{2}{3} \cdot \operatorname{sen}(\sqrt{x}) + C$$

$$24) \int \frac{x^2}{1+x^6} \cdot dx = \int \frac{x^2}{1+(x^3)^2} \cdot dx = \frac{1}{3} \cdot \int \frac{3x^2}{1+(x^3)^2} \cdot dx = \frac{1}{3} \cdot \operatorname{arctg}(x^3) + C$$

$$25) \int \frac{4x}{\cos^2(5x^2-1)} \cdot dx = \frac{4}{10} \cdot \int \frac{10x}{\cos^2(5x^2-1)} \cdot dx = \frac{2}{5} \cdot \operatorname{tg}(5x^2-1) + C$$